Department of Basic Sciences - Philadelphia University

Module Syllabus:

Course Title: Computational Number Theory

Course Code: 250472

Semester: First / 2010–2011
Lecturer: Amin Witno
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Short Description:

This module deals with the computational aspects of elementary number theory, focusing on two main research topics: factorization and primality testing. Public-key cryptography is introduced as a motivational background which also provides contextual applications and examples.

Topics by the Week:

| Week | Topics | | |
|------|--|--|--|
| 1 | The Theory of Divisibility, Prime Numbers and Congruences, Wilson's Theorem | | |
| 2 | The Chinese Remainder Theorem, Fermat's Little Theorem, Euler Phi-Function | | |
| 3 | Modular Exponentiation, Successive Squaring Algorithm, The RSA Cryptosystem | | |
| 4 | Attacks on the RSA, Primitive Roots | | |
| 5 | Quadratic Reciprocity | | |
| 6 | Divisibility Tests, Fermat Factorization, Pollard's Rho Method | | |
| 7 | Pollard p-1 Method, Exponent Factorization, Quadratic Sieve | | |
| 8 | Continued Fractions, Periodic Continued Fractions | | |
| 9 | Factorization using Continued Fractions | | |
| 10 | Pseudoprimes, Carmichael Numbers, Korselt's Criterion | | |
| 11 | Miller-Rabin Test, Strong Pseudoprimes, Rabin's Probabilistic Test | | |
| 12 | Lucas' Converse of Fermat's Little Theorem, Pocklington's Test, Proth's Test | | |
| 13 | Lucas Sequences, Primality Criteria | | |
| 14 | Fermat Numbers, Mersenne Primes and Perfect Numbers | | |
| 15 | Review for Final Exam | | |
| 16 | Final Exam will be held in this period | | |

Mark Distribution:

| • | Exam 1 | 14/11/2010 | 20% |
|---|------------|------------|-----|
| • | Exam 2 | 14/12/2010 | 20% |
| • | Project | TBA | 10% |
| • | Final Exam | TBA | 50% |

Course Notes:

My lecture notes, Computational Number Theory, are required and available for free download from the web site: http://www.philadelphia.edu.jo/math/witno/notes.htm

Textbook:

No textbook is required. A recommended text is the one I have written, Theory of Numbers, BookSurge Publishing 2008. A more excellent book, and more pricely, is David Bressoud's Factorization and Primality Testing, Springer 1980.

Web sites:

- Basic Sciences Department: http://www.philadelphia.edu.jo/math
- Amin Witno Web: http://www.witno.com/
- Number Theory Web: http://www.numbertheory.org/