# Philadelphia University <br> Department of Basic Sciences 

## Exam 2

Set Theory
21-12-2010

Solutions must be complete in order to receive full credit.

1. Prove using induction for all integers $n \geq 1$.

$$
2+4+6+8+\cdots+2 n=n^{2}+n
$$

2. Prove using truth table or Venn diagrams.

$$
(A \oplus B) \oplus B=A
$$

3. Let $A=\{1,2,3,4\}$ and $R=\{(1,1),(1,3),(2,2),(2,4),(3,1),(4,4)\}$. For this relation $R$,
(a) why is reflexive false?
(b) why is symmetric false?
(c) why is anti-symmetric false?
(d) why is transitive false?
4. Let $A=\{0,2,3,6,7,8,10\}$ and $R=\{(a, b) \in A \times A \mid a \bmod 3=b \bmod 3\}$. Prove that $R$ is an equivalence relation on $A$ and find the equivalence classes.
