## Philadelphia University

## Department of Basic Sciences

Choose 4 problems.

1. Complete the quadratic sieve example, $n=119$, given the factorization table.

|  | $11^{2}$ | $16^{2}$ | $22^{2}$ | $25^{2}$ | $27^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 1 | 3 | 1 | - |
| 3 | - | 2 | - | 1 | 1 |
| 5 | - | - | - | 1 | 1 |
| 7 | - | - | - | - | - |

2. Evaluate the periodic infinite continued fraction $[3, \overline{1,4,1}]$. Write the final answer in the form $\frac{P+\sqrt{n}}{Q}$ with $P, Q, n$ integers.
3. Let $p=6 k+1$ and $q=12 k+1$ and $r=18 k+1$ be three prime numbers. Let $n=p \times q \times r$. Prove that $n$ is a Carmichael number.
4. Prove that 121 is a strong pseudoprime with base $a=3$.
5. Prove that 257 is prime using the extended Fermat test, base $a=3$.
-Amin Witno
