## Mathematics I

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Final Exam
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1. Find the derivatives $d y / d x$.
a) $y=\arctan e^{2 x}$
b) $y=\frac{\cos ^{2} x^{3}}{\ln x}$
2. Evaluate the integrals of $f(x) d x$.
a) $f(x)=\frac{e^{\sqrt{x}}}{\sqrt{x}}$
b) $f(x)=\frac{\cos x}{\sin x}$
c) $f(x)=\frac{1}{4+x^{2}}$
3. Sketch the graph given by the parametric equation.

$$
\begin{aligned}
y & =\sin t \\
x & =\cos t \\
\frac{\pi}{2} & \leq t \leq \frac{\pi}{2}
\end{aligned}
$$

4. A coin is tossed 4 times. Draw a table for the binomial probability distribution of the number of Heads.
5. The marks of a Mathematics exam fit a Normal distribution with mean $=12$ and standard deviation $=2$. If 40 students took the exam, estimate how many of them have marks between 9 and 15. You need the value $P(X \leq 1.50)=0.9332$.
6. Find the correlation coefficient and the regression equation for the hypothetical data given below.

| $X$ | $Y$ |
| :--- | :--- |
| ----------- |  |
| 1 | 3 |
| 1 | 5 |
| 2 | 1 |
| 2 | 2 |
| 2 | 3 |

