## PHILADELPHIA UNIVERSITY DEPARTMENT OF BASIC SCIENCES

Exam 2

## Linear Algebra

21 - 12 - 2014

- 1. Let v = (5, -3, 1) and w = (6, 9, -3).
  - (a) Compute the length of v.
  - (b) Compute the length of w.
  - (c) Compute the distance between v and w.
  - (d) Compute the angle between v and w.
- 2. For the matrix A:

 $A = \left[ \begin{array}{rrrr} 1 & 2 & 2 & 4 \\ 3 & 8 & 6 & 16 \\ 0 & 1 & 0 & 2 \end{array} \right]$ 

- (a) Find a basis for the solution space of A.
- (b) Find a basis for the column space of A.
- 3. Consider the vectors in  $\{(1, 1, 1), (1, 2, 3), (1, 4, 9)\}$ .
  - (a) Do they span or not span  $R^3$ ?
  - (b) Are they linearly dependent or independent?
  - (c) Do they form a basis for  $R^3$ ?
- 4. Given the old basis  $\{(0,2), (2,0)\}$  and the new basis  $\{(1,1), (-1,1)\}$  for  $\mathbb{R}^2$ :
  - (a) Find the matrix of transition from the old to the new basis.
  - (b) Find the new coordinates of the old point (3, 5).
  - (c) Find the old coordinates of the new point (2, 2).
- 5. Change the basis  $\{(2, 2, 1), (-2, 1, 2), (2, 0, 0)\}$  for  $\mathbb{R}^3$  to an orthonormal basis using the Gram-Schmidt process. Hint: recall the formula

new 
$$v_3 = v_3 - (v_3 \cdot v_1)v_1 - (v_3 \cdot v_2)v_2$$